

Semester Two Examination, 2019

Question/Answer booklet

MATHEMATICS SPECIALIST UNITS 3 AND 4

Section Two:

Calculator-assumed

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Student number:	In figures				
	In words	 			
	Your name				

Time allowed for this section

Reading time before commencing work: ten minutes

Working time: one hundred minutes

Materials required/recommended for this section

To be provided by the supervisor

This Question/Answer booklet Formula sheet (retained from Section One)

To be provided by the candidate

Standard items: pens (blue/black preferred), pencils (including coloured), sharpener,

correction fluid/tape, eraser, ruler, highlighters

Special items: drawing instruments, templates, notes on two unfolded sheets of A4 paper,

and up to three calculators approved for use in this examination

Important note to candidates

No other items may be taken into the examination room. It is **your** responsibility to ensure that you do not have any unauthorised material. If you have any unauthorised material with you, hand it to the supervisor **before** reading any further.

Structure of this paper

Section	Number of questions available	Number of questions to be answered	Working time (minutes)	Marks available	Percentage of examination
Section One: Calculator-free	8	8	50	54	35
Section Two: Calculator-assumed	13	13	100	100	65
				Total	100

Instructions to candidates

- 1. The rules for the conduct of examinations are detailed in the school handbook. Sitting this examination implies that you agree to abide by these rules.
- 2. Write your answers in this Question/Answer booklet preferably using a blue/black pen. Do not use erasable or gel pens.
- 3. You must be careful to confine your answer to the specific question asked and to follow any instructions that are specified to a particular question.
- 4. Show all your working clearly. Your working should be in sufficient detail to allow your answers to be checked readily and for marks to be awarded for reasoning. Incorrect answers given without supporting reasoning cannot be allocated any marks. For any question or part question worth more than two marks, valid working or justification is required to receive full marks. If you repeat any question, ensure that you cancel the answer you do not wish to have marked.
- 5. It is recommended that you do not use pencil, except in diagrams.
- 6. Supplementary pages for planning/continuing your answers to questions are provided at the end of this Question/Answer booklet. If you use these pages to continue an answer, indicate at the original answer where the answer is continued, i.e. give the page number.
- 7. The Formula sheet is not to be handed in with your Question/Answer booklet.

Section Two: Calculator-assumed

65% (100 Marks)

This section has **thirteen (13)** questions. Answer **all** questions. Write your answers in the spaces provided.

Working time: 100 minutes.

Question 9 (5 marks)

Solve the equation $z^5 = 16 + 16\sqrt{3}i$, giving solutions in polar form $r \operatorname{cis} \theta$ where $-\pi < \theta \le \pi$ and r > 0.

Solution
$$z^{5} = 32 \operatorname{cis}\left(\frac{\pi}{3}\right)$$

$$z_{k} = \sqrt[5]{32} \operatorname{cis}\left(\frac{\pi}{3} \times \frac{1}{5} + \frac{2n\pi}{5}\right)$$

$$z_{k} = 2 \operatorname{cis}\left(\frac{\pi}{15} + \frac{2n\pi}{5}\right), n = -2, -1, 0, 1, 2$$

$$z_{1} = 2 \operatorname{cis}\left(-\frac{11\pi}{15}\right)$$

$$z_{2} = 2 \operatorname{cis}\left(-\frac{\pi}{3}\right)$$

$$z_{3} = 2 \operatorname{cis}\left(\frac{\pi}{15}\right)$$

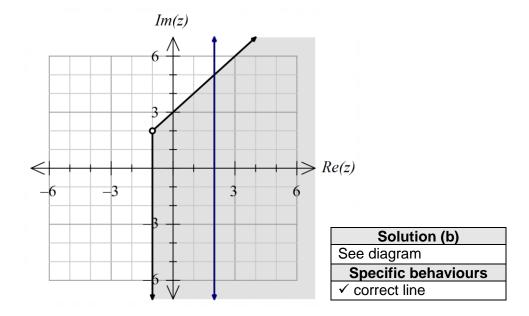
$$z_{4} = 2 \operatorname{cis}\left(\frac{7\pi}{15}\right)$$

$$z_{5} = 2 \operatorname{cis}\left(\frac{13\pi}{15}\right)$$

- ✓ converts to polar form
- ✓ applies de Moivre's
- ✓ one correct root
- √ three correct roots
- ✓ all correct roots

Question 10 (4 marks)

The locus of a complex number z is shown below.



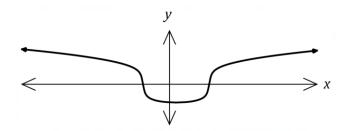
(a) Without using Re(z) or Im(z), write an inequality in terms of z for the locus. (3 marks)

Solution	
$-\frac{\pi}{2} \le \arg(z - (-1 + 2i)) \le \frac{\pi}{4}$	
Specific behaviours	
✓ lower argument	
✓ upper argument	
✓ translation	

(b) Add the locus for |z| = |z - 4| to the diagram above. (1 mark)

Question 11 (6 marks)

A particle is moving along the curve shown below with equation $x^2 - x = y^5 + y + 6$.



The x-coordinate of the particle is changing at a constant rate given by $\frac{dx}{dt} = -2$.

Determine the rate/s at which the y-coordinate of the particle is changing when y = 0.

$$2x - 1 = 5y^4 \frac{dy}{dx} + \frac{dy}{dx}$$

$$y = 0 \Rightarrow \frac{dy}{dx} = 2x - 1$$

$$\frac{dy}{dt} = \frac{dy}{dx} \frac{dx}{dt}$$
$$= -2(2x - 1)$$

$$y = 0 \Rightarrow x^2 - x - 6 = 0$$
$$(x - 3)(x + 2) = 0$$

At
$$(3,0)$$
, $\frac{dy}{dt} = -2(5) = 10$

At
$$(-2,0)$$
, $\frac{dy}{dt} = -2(-5) = 10$

Specific behaviours

- ✓ implicitly differentiates wrt x
- ✓ expression for dy/dx
- ✓ expression for dy/dt
- ✓ determines x when y = 0
- ✓ one correct rate
- ✓ both correct rates

Alternative part solution
$$2x\frac{dx}{dt} - \frac{dx}{dt} = 5y^4 \frac{dy}{dt} + \frac{dy}{dt}$$

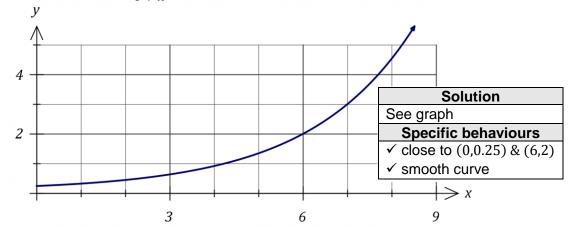
$$y = 0$$
, $\frac{dx}{dt} = -2$

$$\frac{dy}{dt} = -2(2x - 1)$$

- ✓ implicitly differentiates LHS wrt t
- √ implicitly differentiates RHS wrt t
- \checkmark expression for dy/dt

Question 12 (5 marks)

Sketch the graph of $y = \frac{e^{0.5x}}{4+x}$ on the axes below. (a) (2 marks)



The Trapezoidal Rule can be used to determine the numerical approximation of a definite integral when an antiderivative cannot be found. When a continuous interval $[a_0, a_n]$ is divided into nsmaller intervals of equal width w, the bounds of these smaller intervals can be denoted by a_0 , a_1 , a_2 ,..., a_{n-1} , a_n . The Trapezoidal Rule is then expressed as follows:

$$\int_{a_0}^{a_n} f(x) \, dx = \frac{w}{2} [f(a_0) + 2f(a_1) + 2f(a_2) + \dots + 2f(a_{n-1}) + f(a_n)]$$

Use the above rule to determine an estimate to 4 decimal places for $\int_0^8 \frac{e^{0.5x}}{4+x} dx$ (b) using 4 intervals. (3 marks)

Solution
$\frac{2}{2}(f(0) + 2f(2) + 2f(4) + 2f(6) + f(8))$ = 11.5702
Specific behaviours
✓ indicates use of rule with correct intervals

- ✓indicates use of correct values ✓ correct estimate, to 4 dp

Question 13 (8 marks)

The diameter of copper wire produced by a machine is normally distributed with a mean of 545 μ m and a variance of 357 μ m².

A production supervisor routinely takes a random sample of 36 diameters and calculates their mean, \bar{X} .

(a) Describe the distribution of \bar{X} .

(3 marks)

Solution
$ar{X}$ is normally distributed
$357 \div 36 = 9.917$
$\bar{X} \sim N(545, 9.917) \sim N(545, 3.149^2)$
Specific behaviours

- √ states normally distributed
- ✓ states mean
- √ states variance (or sd)

Determine the probability that the mean of a random sample of 36 diameters is less than (b) (1 mark) 540 μm.

Solution
$$P(\bar{X} < 540) = 0.0562$$
Specific behaviours
$$\checkmark \text{ correct probability}$$

Repeated random sampling of n diameters from the machine shows that there is a 21% (c) chance that the sample mean exceeds 547 μm . Determine n. (4 marks)

Solution 1
$\bar{Y} \sim N\left(545, \frac{357}{n}\right)$
$P(\bar{Y} > 547) = 0.21$
$\sqrt{\frac{357}{n}} = 2.480$
n = 58
Specific behaviours
✓ writes distribution

√ writes probability statement

 \checkmark writes equation for n

✓ correct value of n

n = 58Specific behaviours ✓ writes distribution

 $\overline{Y} \sim N\left(545, \frac{357}{n}\right)$

 $P(Z > k) = 0.21 \Rightarrow k = 0.8064$

 $\frac{547 - 545}{\sqrt{357 \div n}} = 0.8064$

- ✓ indicates use of z-score, k ✓ writes equation for n
- ✓ correct value of n

Question 14 (9 marks)

A virus, that eventually leads to death in just feral cats, is to be released in a large nature reserve where the cats are having a devastating effect on native animals. From previous data, it is

expected the rate at which the virus spreads will be modelled by $\frac{dV}{dt} = \frac{V}{10} - \frac{V^2}{800}$

where V is the number of feral cats with the virus and t is the time in days. Five feral cats are initially infected with the virus.

(a) What form of relationship does this differential equation model? (1 mark)

Solution	
Logistic	
Specific behaviours	
✓ gives correct response	

(b) Express V as a function of t in the form $V = \frac{K}{1 + Ce^{-at}}$ (4 marks)

Solution
$K = \frac{1}{10} \div \frac{1}{800} = 80$ $a = \frac{1}{10} \implies V = \frac{80}{1 + Ce^{-0.1t}}$
$t = 0, V = 5 \implies 5 = \frac{80}{1+C} \implies C = 15$
$V = \frac{80}{1 + 15e^{-0.1t}}$

- √ determines value for a
- √ determines value for K
- √ determines value for C
- √ writes equation for V
- (c) Determine the expected number of feral cats to have the virus after two weeks of its release. (1 mark)

Solution
$$t = 14 \implies V = 17$$
Specific behaviours
$$\checkmark \text{ gives correct solution}$$

(d) For what value/s of V is the growth rate zero?

(1 mark)

Solution
$\frac{V}{10} - \frac{V^2}{800} = 0 \implies V = 0.80$
Specific behaviours
✓ gives correct solution

(e) Determine the time taken to when 75% of the feral cat population are expected have the virus. (2 marks)

Solution
$60 = \frac{80}{1 + 15e^{-0.1t}} \implies t = 38 days$
Specific behaviours
✓ uses correct cat population of 60
√calculates correct answer

Question 15 (8 marks)

A researcher used data from a sample of 125 newborn babies in order to estimate the mean weight and length of newborns in a large city.

- (a) The weights of the babies in the sample had a mean of 3.28 kg and a standard deviation of 0.62 kg.
 - (i) Use this data to obtain a 95% confidence interval for the mean weight of a newborn baby in the city. (2 marks)

Solution	
(3.171, 3.38	9)
Specific behave	iours
Specific behav ✓ lower bound	riours

(ii) State two assumptions made when constructing your confidence interval. (2 marks)

Solution			
Sample was obtained randomly			
Sample values are independent of each other			
Sample means are normally distributed			
Specific behaviours			
√ first assumption			
✓ second assumption			

(b) The 99% confidence interval for the mean length L cm of newborn babies derived from the sample was (49.88, 50.92). Determine the sample mean and standard deviation used to construct this interval. (4 marks)

Solution
$$E = \frac{50.92 - 49.88}{2} = 0.52$$

$$\bar{x} = 49.88 + 0.52 = 50.4$$

$$2.576 \times \frac{s}{\sqrt{125}} = 0.52$$

$$s = 2.257 \text{ cm}$$
Specific behaviours
$$\checkmark \text{ margin of error}$$

$$\checkmark \text{ mean}$$

$$\checkmark \text{ equation for sd}$$

$$\checkmark \text{ standard deviation}$$

Question 16 (6 marks)

(a) State the equations of all asymptotes of the graph of
$$y = \frac{72 - 5x^2}{x^2 - 36}$$
. (2 marks)

Solution y = -5 $x = 6, \quad x = -6$ Specific behaviours $\checkmark \text{ horizontal asymptote}$

✓ both vertical asymptotes

(b) Let
$$f(x) = \frac{ax^2 + bx + c}{x + d}$$
.

The graph of y = f(x) has a y-intercept of -9, two asymptotes (with equations x = -1 and y = 5 - 2x) and no roots. Determine the value of each of the constants a, b, c and d.

(4 marks)

Solution

$$y = 5 - 2x + \frac{k}{x+1}$$

$$x = 0, y = -9 \Rightarrow -9 = 5 + k \Rightarrow k = -14$$

$$y = 5 - 2x - \frac{14}{x+1}$$

$$= \frac{(5 - 2x)(x+1) - 14}{x+1}$$

$$= \frac{-2x^2 + 3x - 9}{x+1}$$

$$a = -2, \quad b = 3, \quad c = -9, \quad d = 1$$

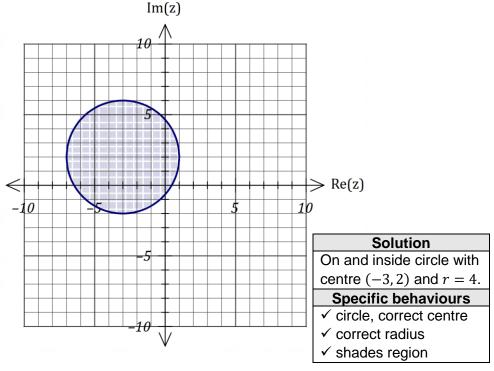
Specific behaviours

- ✓ uses asymptotes to form equation
- ✓ uses intercept to determine k
- ✓ combines into single fraction
- ✓ correctly states all four values

(Max ✓✓ if b incorrect)

Question 17 (9 marks)

(a) Indicate the subset of points in the complex plane that satisfy $|z + 3 - 2i| \le 4$ on the axes below. (3 marks)



- (b) Given that $|z + 3 2i| \le 4$, determine
 - (i) the maximum value of Im(z).

Solution
Maximum is 6.
Specific behaviours
✓ real answer
✓ correct value

(ii) the minimum value of |z-2|.

(2 marks)

(2 marks)

Solution

Require minimum distance from (2,0) to point on circle - will lie on ray from centre.

$$\sqrt{5^2 + 2^2} - 4 = \sqrt{29} - 4 \approx 1.39$$

Specific behaviours

- √ indicates correct method
- √ correct value

(iii) the minimum value of Re(iz).

(2 marks)

Solution

Re(iz) = -Im(z)Hence minimum value is -6.

Specific behaviours

- ✓ indicates correct method
- √ correct value

See next page

Question 18 (12 marks)

Points A, B and C lie in plane Π and have position vectors $\begin{pmatrix} 10 \\ 0 \\ 5 \end{pmatrix}$, $\begin{pmatrix} 3 \\ -2 \\ -3 \end{pmatrix}$ and $\begin{pmatrix} 5 \\ -3 \\ 4 \end{pmatrix}$ respectively. Point B also lies on the sphere S that has centre A.

(a) Determine the vector equation of S.

(3 marks)

Solution $\overrightarrow{AB} = \begin{pmatrix} 3 \\ -2 \\ -3 \end{pmatrix} - \begin{pmatrix} 10 \\ 0 \\ 5 \end{pmatrix} = \begin{pmatrix} -7 \\ -2 \\ -8 \end{pmatrix}$ $|\overrightarrow{AB}| = 3\sqrt{13}$ $\begin{vmatrix} \mathbf{r} - \begin{pmatrix} 10 \\ 0 \\ 5 \end{pmatrix} \end{vmatrix} = 3\sqrt{13}$

- Specific behaviours
- ✓ vector \overrightarrow{AB}
- √ calculates radius
- ✓ states vector equation

(b) Determine the Cartesian equation for plane Π .

(4 marks)

Solution
$$\overrightarrow{AC} = \begin{pmatrix} 5 \\ -3 \\ 4 \end{pmatrix} - \begin{pmatrix} 10 \\ 0 \\ 5 \end{pmatrix} = \begin{pmatrix} -5 \\ -3 \\ -1 \end{pmatrix}$$

$$\overrightarrow{AB} \times \overrightarrow{AC} = \begin{pmatrix} -22 \\ 33 \\ 11 \end{pmatrix}$$

$$\mathbf{n} = \begin{pmatrix} 2 \\ -3 \\ -1 \end{pmatrix}$$

$$\overrightarrow{OA} \cdot \mathbf{n} = \begin{pmatrix} 10 \\ 0 \\ 5 \end{pmatrix} \cdot \begin{pmatrix} 2 \\ -3 \\ -1 \end{pmatrix} = 15$$

$$2x - 3y - z = 15$$
Specific behaviours

- \checkmark vector \overrightarrow{AC} or \overrightarrow{BC} , etc
- √ uses cross product to obtain normal
- ✓ uses dot product to obtain constant
- √ states Cartesian form

A point and its reflection in a plane are equidistant from the plane and lie on a line that is perpendicular to the plane.

Point *P* has position vector $\begin{pmatrix} -6\\14\\1 \end{pmatrix}$.

(c) Determine the position vector of P', the reflection of P in plane Π .

(5 marks)

Solution

Line through P perpendicular to plane:

$$\mathbf{r} = \begin{pmatrix} -6\\14\\1 \end{pmatrix} + \lambda \begin{pmatrix} 2\\-3\\-1 \end{pmatrix}$$

Line intersects plane at Q, when:

$$\begin{bmatrix} \begin{pmatrix} -6\\14\\1 \end{pmatrix} + \lambda \begin{pmatrix} 2\\-3\\-1 \end{pmatrix} \end{bmatrix} \cdot \begin{pmatrix} 2\\-3\\-1 \end{pmatrix} = 15$$

$$2(-6+2\lambda) - 3(14-3\lambda) - (1-\lambda) = 15$$

 $\lambda = 5$

Hence $\overrightarrow{OQ} = \mathbf{r}(5)$ and so $\overrightarrow{OP'} = \mathbf{r}(10)$:

$$\overrightarrow{OP'} = \begin{pmatrix} -6\\14\\1 \end{pmatrix} + 10 \begin{pmatrix} 2\\-3\\-1 \end{pmatrix} \\
= \begin{pmatrix} 14\\-16\\-9 \end{pmatrix}$$

- √ writes equation of line through P
- ✓ substitutes line into plane
- ✓ solves for λ
- ✓ indicates method to determine P'
- ✓ correct position vector for P'

Question 19 (9 marks)

Researchers used a simulation to model the population of foxes F(t) and the population of rabbits R(t) on an island. The rates of change of each population after t years are given by

$$\frac{dF}{dt} = 0.5R$$
 and $\frac{dR}{dt} = -0.125F$.

Briefly explain how the rabbit population is changing. (a)

(1 mark)

Solution

Rabbit population is decreasing at a rate proportional to the population of foxes.

Specific behaviours

✓ states decreasing

Show that $\frac{d^2F}{dt^2} = -0.0625F$. (b) (2 marks)

Solution
$$\frac{d}{dt} \left(\frac{dF}{dt} \right) = \frac{d}{dt} (0.5R)$$

$$\frac{d^2F}{dt^2} = 0.5 \frac{dR}{dt}$$
= 0.5(-0.125F)
= -0.0625F

Specific behaviours

√ differentiates both sides

✓ substitutes and simplifies

The equation in part (b) suggests that a model of the form $F(t) = k \sin(at + b)$ would be appropriate, where a, b and k are positive constants.

(c) Explain this choice of model. (1 mark)

Solution

The equation in (b) is of the form

$$F^{\prime\prime} = -a^2 F$$

and represents simple harmonic motion.

Specific behaviours

√ indicates SHM

The research model used b = 0.15 and the initial size of the fox population was 700.

(d) Determine the value of a and the value of k.

(2 marks)

$$a^2 = 0.0625 \Rightarrow a = 0.25$$

$$700 = k \sin(0.15) \Rightarrow k = 4684$$

Specific behaviours

- \checkmark value of a
- ✓ value of k

(e) Determine an equation for R(t) in terms of t and use it to calculate the number of years until the rabbit population becomes extinct. (3 marks)

Solution

$$\frac{dF}{dt} = 0.5R \Rightarrow R = 2\frac{dF}{dt}$$

$$F(t) = 4684\sin(0.25t + 0.15)$$

$$\frac{dF}{dt} = 1171\cos(0.25t + 0.15)$$

$$R(t) = 2(1171)\cos(0.25t + 0.15)$$

$$R(t) = 2342\cos(0.25t + 0.15)$$

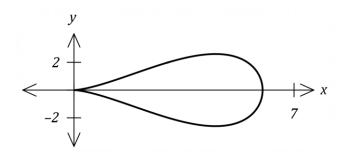
$$R(t) = 0 \Rightarrow t = 5.68 \text{ years}$$

- ✓ obtains F'(t)
- ✓ obtains R(t)
- ✓ correct time

(1 mark)

Question 20 (11 marks)

The path of a particle is shown in the diagram below.



The position vector of the particle after t seconds is given by $\mathbf{r}(t) = \begin{pmatrix} 3 - 3\sin t \\ 2\cos t - \sin 2t \end{pmatrix}$ centimetres, for $t \ge 0$.

(a) Determine the initial position of the particle.

Solution			
$\mathbf{r}(0) = \binom{3}{2} \text{ cm}$			
Specific behaviours			
✓ correct position			

(b) Determine the acceleration vector of the particle at the instant it first reaches the origin.

(4 marks)

Solution			
$x = 0 \Rightarrow 3 - 3\sin t = 0 \Rightarrow t = \frac{\pi}{2}$			
$\mathbf{v}(t) = \begin{pmatrix} -3\cos t \\ -2\sin t - 2\cos 2t \end{pmatrix}$			
$\mathbf{a}(t) = \begin{pmatrix} 3\sin t \\ -2\cos t + 4\sin 2t \end{pmatrix}$			
$\mathbf{a}\left(\frac{\pi}{2}\right) = \binom{3}{0} \text{ cm s}^{-2}$			
Specific behaviours			

- √ indicates time
- √ velocity vector
- √ acceleration vector
- ✓ substitutes and simplifies

(c) Determine the distance travelled by the particle from the time it leaves its initial position until the time it first reaches the origin. (3 marks)

Solution
$$|\mathbf{v}(t)| = \sqrt{(-3\cos t)^2 + (-2\sin t - 2\cos 2t)^2}$$

$$s = \int_0^{\frac{\pi}{2}} |\mathbf{v}(t)| dt$$

$$s \approx 3.629 \text{ cm}$$

- Specific behaviours
- √ expression for magnitude of velocity
- √ forms correct integral
- √ correct distance
- (d) The Cartesian equation of the path of the particle is $ay^2 + bx^3 + 4x^4 = 0$. Determine the value of each of the constants a and b. (4 marks)

Solution

$$y = 2 \cos t - 2 \cos t \sin t$$

$$= 2 \cos t (1 - \sin t)$$

$$x = 3 - 3 \sin t \Rightarrow \frac{x}{3} = 1 - \sin t$$

$$y = 2 \cos t \left(\frac{x}{3}\right)$$

$$3y = 2x \cos t$$

$$9y^{2} = 4x^{2} \cos^{2} t$$

$$= 4x^{2} (1 - \sin^{2} t)$$

$$\sin t = \frac{x}{3} - 1 \Rightarrow \sin^{2} t = \left(\frac{x}{3} - 1\right)^{2} = \frac{x^{2}}{9} - \frac{2x}{3} + 1$$

$$9y^{2} = 4x^{2} \left(1 - \frac{x^{2}}{9} + \frac{2x}{3} - 1\right)$$

$$9y^{2} = \frac{8x^{3}}{3} - \frac{4x^{4}}{9}$$

$$81y^{2} = 24x^{3} - 4x^{4} \Rightarrow a = 81, b = -24$$

- \checkmark obtains relation between x, y and $\cos t$
- ✓ obtains relation for $\sin^2 t$ in terms of x
- √ eliminates all trig terms
- √ correct values for constants

Question 21 (7 marks)

Water, containing 6 grams of dissolved sugar per litre, flows into a tank at a constant rate of 10 litres per hour.

Water is drawn from the tank, initially containing 250 litres of water with no dissolved sugar, at the same constant rate of 10 litres per hour.

Let the weight of sugar in the tank after t hours be w grams and assume that the sugar is always evenly dissolved throughout the water in the tank.

(a) By considering the rate at which dissolved sugar flows in and out of the tank, show that

(2 marks)

$$\frac{dw}{dt} = \frac{1500 - w}{25}.$$

Solution			
Rate out: $10 \times \frac{w}{250} = \frac{w}{25}$			
Rate in: $10 \times 6 = 60$			
$\frac{dw}{dt} = 60 - \frac{w}{25} = \frac{1500 - w}{25}$			

Specific behaviours

- √ derives rate out
- ✓ derives rate in and uses difference

The water drawn from the tank can be used in a manufacturing process once the level of dissolved sugar exceeds 0.75 grams per litre.

(b) Derive an equation for w in terms of t and hence determine how long this will take.

(5 marks)

Solution
$\int \frac{1}{1500 - w} dw = \int \frac{1}{25} dt$
$-\ln(1500 - w) = \frac{t}{25} + c$
$1500 - w = ke^{-0.04t}$
$t = 0, w = 0 \Rightarrow k = 1500$ $w = 1500(1 - e^{-0.04t})$
$0.75 \times 250 = 1500(1 - e^{-0.04t})$ t = 3.338 h Will take 3 hours 20 minutes.

- √ separates variables
- ✓ integrates both sides, shows constant
- √ eliminates logs
- √ correct equation
- ✓ solves for t

Supplementary page					
Question number:					

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SEMESTER 2 2019 CALCULATOR ASSUMED

Supplementary page	
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